

# Climate Change Calculated 2

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Question: Does the CO<sub>2</sub> concentration influence the global temperature?

- **Physics:**
- Significant effect: Absorption spectra of CO<sub>2</sub> and water vapor:
- [https://en.wikipedia.org/wiki/Radiative\\_forcing](https://en.wikipedia.org/wiki/Radiative_forcing)
- Water vapor is short lived and dependent on temperature, hence CO<sub>2</sub> is the primary gas.
- We see:
- CO<sub>2</sub> is **transparent** to the electromagnetic spectrum of **visible light**,
- but it **absorbs** in the **range of infrared**, ie the heat radiation
- The sun heats up the earth with the visible light,
- heat is radiated back into space as infrared radiation.

- This is how a balance is established.

## The Radiative Forcing of CO2

- More CO2 in the atmosphere keeps more infrared radiation on Earth.
- This additional retained radiation is called "**radiative forcing**"  
([https://en.wikipedia.org/wiki/Radiative\\_forcing](https://en.wikipedia.org/wiki/Radiative_forcing))
- Formula of radiative forcing of CO2:

$$\Delta F = 5,35 \frac{\text{W}}{\text{m}^2} \cdot \ln \frac{C}{C_0}$$

- $C_0$  : CO2 reference, 280ppm of the pre-industrial time,
- C: new CO2 value, 410ppm (2019)
- The result is a power in watts per unit area  $\text{m}^2$
- In Python:

```
import numpy as np  
  
5.35 * np.log (410/280)
```

- Result: **2.04 W / m<sup>2</sup>**
- CO2 radiative forcing thus is approx. 2W / m<sup>2</sup> (+- ca. 10%)

- This is the **additional power** from the increase of CO<sub>2</sub> to 410ppm compared to the pre-industrial level of 280ppm.
- This is about the power of a bicycle lamp for every square meter of the earth.
- Variations of the solar radiation come to about 0.5W / m<sup>2</sup>
- Other effects are even lower
- -> The radiative forcing of CO<sub>2</sub> is the dominating effect

**Question: How long does it take for the radiative forcing to heat up earth by 1 degree C (1.8F)?**

- The earth is **dominated by oceans**, accounting for 70% of the surface
- Therefore, we focus on the **oceans for our estimation**
- The **heat capacity** of water is the energy needed to warm up 1kg of water by 1 degree Celsius (or Kelvin).
- Unit: J / (kg \* K) = (Ws) / (kg \* K)
- Heat capacity of water: **c = 4.2 \* 10<sup>3</sup> J / (kg \* K)**  
([https://en.wikipedia.org/wiki/Table\\_of\\_specific\\_heat\\_capacities](https://en.wikipedia.org/wiki/Table_of_specific_heat_capacities))
- Water also has a higher heat capacity than earth
- We can now transform the units of heat capacity to obtain the formula for the time for 1 degree warming:

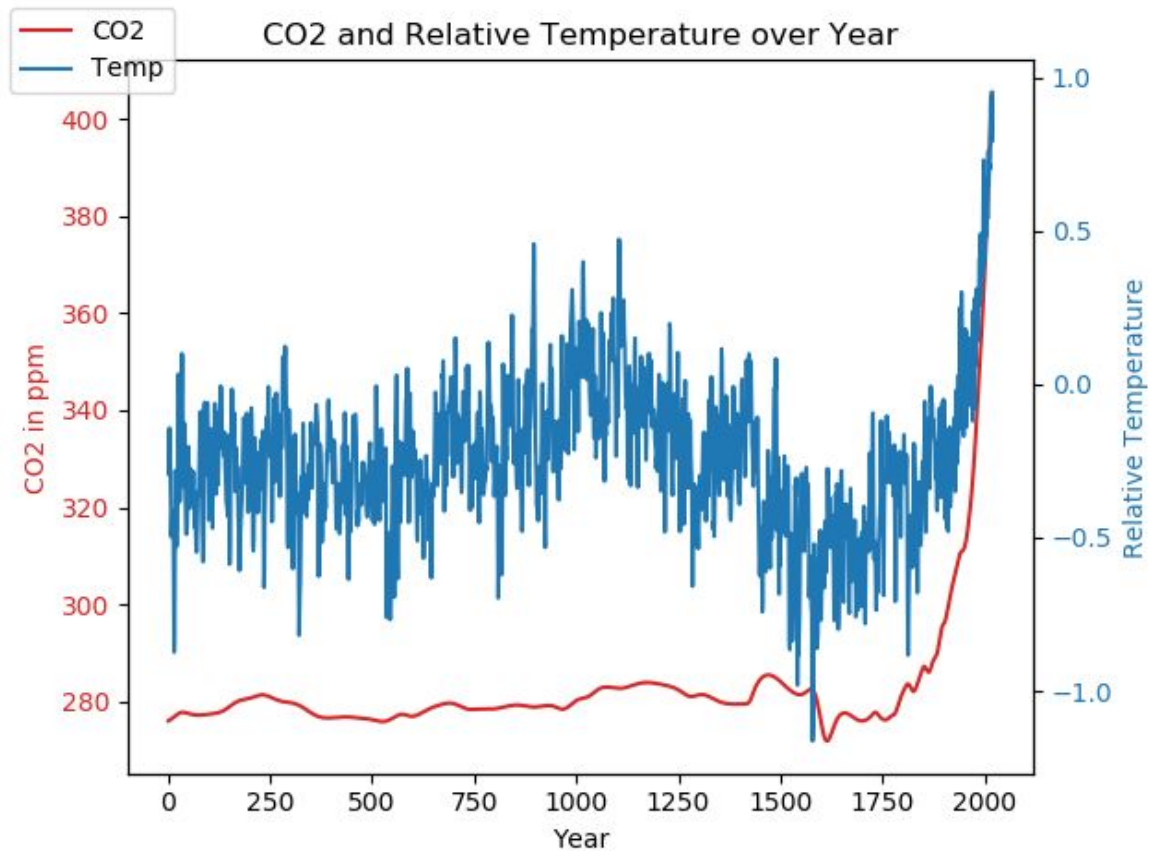
- $c = \frac{Ws}{kg \cdot K}$  , hence:
- $\frac{c \cdot kg}{W} = \frac{s}{K}$
- Unit of right side: s / K, ie **seconds per Kelvin**
- This is the time in seconds needed for 1 degree temperature increase (Kelvin or Celsius).
- For every square meter of ocean we get the mentioned 2W radiative forcing
- But to what **depth** do we have to consider the oceans?
- The so-called "thermocline" is a kind of insulating boundary layer to the deep sea.
- <https://de.wikipedia.org/wiki/Thermokline>
- It extends roughly from 200-1000m depth in the oceans.
- Let's assume the middle of the layer at **600m** as the limit to which energy penetrates from the surface.
- Water has a mass of 1000 kg per cubic meter
- For each square meter and 600m water depth we have a water mass of 600m \* 1000 kg / m<sup>3</sup> = **600000 kg / m<sup>2</sup>**
- We insert this mass of 600000 kg / m<sup>2</sup> in our formula for the time per Kelvin and expand it with 1/m<sup>2</sup>:
- $\frac{s}{k} = \frac{c \cdot kg}{W} = \frac{c \cdot kg / m^2}{W / m^2}$
- This leads to:
- $s / K = 4.2 * 10^3 J / (kg * K) * 600000 kg / m^2 / (2 W / m^2)$   
 $= (4.2e3 * 600e3 / 2) s / K$
- $= 1260000000.0 s / K = \mathbf{1.26e9 s / K}$
- This is now the time in seconds for 1 degree temperature increase. We can convert this to years by dividing by the number of seconds per year.

- 1 year =  $60 \cdot 60 \cdot 24 \cdot 365$  s = 31536000 s = 31.536e6 s
- So:  $1.26e9$  s/K =  $1.26e9 / 31.536e6$  years/K
- = **39.95 years**
- **Over the last 40 years (1980-2019) we indeed had an increase of global temperature of about 1 degree Celsius (shown next), so this is a good fit.**

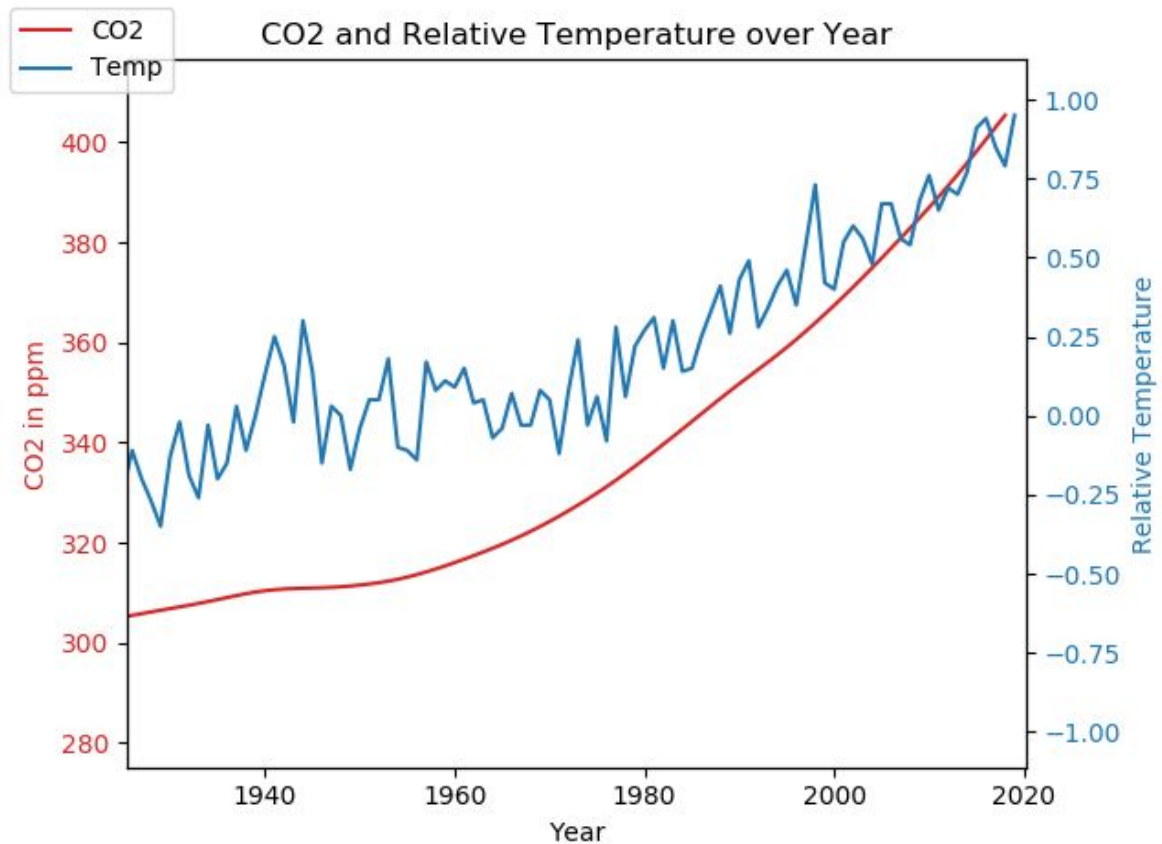
## Historical temperature values

- We can obtain global temperature values, as relative temperatures (they are more accurate than absolute values), from 1880 to present as a csv file:
- [https://www.ncdc.noaa.gov/cag/global/time-series/globe/land\\_ocean/1/6/1880-2019.csv](https://www.ncdc.noaa.gov/cag/global/time-series/globe/land_ocean/1/6/1880-2019.csv)
- For the last 1000 years:
- <https://www.temperaturerecord.org>
- Below is a link for the last 2,000 years that we store and convert to csv:
- historical\_temperature\_dataset\_0-1979\_py.csv
- We combine both datasets using a Python Program, and plot it, along with the CO2 values.
- We start the program in the terminal with:
  - `python3 dataplot_twinplot2.py`
- The blue curve represents the combined temperature data

- The red curve is the CO2 data for comparison
- We see: our **today's deviation** of the temperature from the annual mean is already **bigger than during the "small ice age"** in the Medieval Age, and **much warmer than at the time of the Roman empire!**



- We can zoom in on the modern times and see:
- From about 1980 we have a **temperature increase of about 1 degree, as we calculated!**



## Conclusion

- Our estimation shows that the global **temperature rise is caused by the increased CO2 concentration.**
- With the further emissions of fossil CO2, the radiative forcing will continue to increase, and the **temperature rise will accelerate.**