Automatic Calibration of Multiple Stationary Laser Range Finders using Trajectories

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Abstract

Laser based detection and tracking of persons can be used for numerous tasks, like statistical measurements for determining bottlenecks in public buildings, optimizing passenger flow, or planning camera placement. Only a network of multiple LRF is sufficient to fulfill these tasks in larger spaces. Calibrating multiple LRF into a global coordinate system is usually done by hand in a time consuming procedure. In this paper, we address the problem of automatically calibrating such a sensor network. We introduce an automatic calibration mechanism, which is able to obtain the positions and orientations of all LRF in a global coordinate system, without any prior knowledge of the scene. Our approach is based on comparing person tracks, determined by each individual LRF unit and matching them in order to obtain constraints between the LRF units. By resolving these constraints, we are able to estimate the poses of all LRF. We evaluate and compare our method to the current state of the art approach methodically and experimentally. Experiments show that our calibration approach outperforms this approach.

1. Introduction

Detecting and tracking people with laser range finders (LRF) yield a lot of applications in the field of surveillance. The utilization vary from simple statistical measurements, like determining bottlenecks in public buildings and optimizing passenger flows, up to more sophisticated tasks, such as detecting irregular behaviors [13]. Additionally, tracking persons with laser range finders does not violate personal rights and puts privacy law advocates at ease to a certain degree.

Using only one static LRF limits the area for tracking to its maximum detection range. Also occlusions may disturb the tracking. Both problems can be avoided by adding more LRF to the scene. However by doing so, a new problem comes up: all laser range finders need to be calibrated into one global coordinate system in order to continuously track persons over larger distances. This can be done by measuring their position and orientation by hand. Since this procedure is very time consuming, we present a calibration algorithm, which is able to automatically determine the positions and orientations of all laser range finders in a global coordinate system without any prior knowledge of the scene.

The remainder of this paper is organized as following: We present the state of the art for matching static and dynamic objects for calibration in Sect. 2, followed by the description of the calibration algorithm in Sect. 3. Additionally, we benchmark our approach and compare it to the state of the art in various challenging setups in Sect. 4. Finally, we are summarizing the results in Sect. 5 and giving an outlook.

2. State of the Art

Calibration of a sensor network with unknown topology is a common problem. For multiple LRF, three categories for estimating their positions can be applied. First, approaches known in mobile robotics may be adopted for calibration (Sect. 2.1). Second, static objects in scan data can be matched to align all laser range finder (Sect. 2.2). Third, dynamic objects observed in scan data over time are applicable for matching (Sect. 2.3).

2.1. Robotic Matching Techniques

In mobile robotics, localization in an unknown environment is a similar problem to calibration of a sensor network. As the robot moves through the scene, scan data from different locations can be regarded as scans from different sensors

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Figure 1. General workflow of the proposed calibration method. First, all persons are tracked for each single LRF. Afterwards, tracks between the LRF are associated. After pairing all sensors with constraints, their poses are initially estimated. In order to take every constraint into account, a relaxation algorithm is applied. Finally, the LRF are aligned on static background objects with ICP.

in a sensor network. SLAM or other robot matching techniques [6, 14] can be used to resolve their positions. Unfortunately these techniques are only applicable for robots, since the relative positions between multiple observations are known from odometry information. When using a network of stationary sensors, the relative distances between different sensors are unknown, so robot localization methods are not applicable for the scenario of stationary sensors.

2.2. Matching of static objects

Static objects, which can be observed by multiple laser range finders, can be used as reference objects for calibration. Scan matching methods, like Iterative Closest Point (ICP) [1], Polar Scan Matching (PSM) [2], or others [15, 16, 21], can be used to rectify the sensors. Also point registration methods from computer vision are applicable [9]. As stated in [5] the use of scan matching techniques should be avoided in our scenario, since several problems exist:

- occlusions, caused by obstacles or disadvantageous arrangements
- ambiguities and symmetries in the environment may lead to false matches
- no static object may exist, which is mutually observed by multiple LRF

Another possibility to calibrate multiple LRF is to add markers to the sensors (e.g. reflectors for laser range finders) and use them as landmarks. In this case, irresolvable ambiguities or obstacles can disturb the alignment. In general, matching with static objects is not preferable as calibration method as long as no initial hypothesis is available.

2.3. Matching of dynamic objects

Dynamic objects, as for example persons walking through the scene, can be used for calibration as well. Based on tracking all persons individually for each LRF, a calibration algorithm was presented in [5] and [17]. These

algorithms use several randomly picked pairs of observations of the same person to estimate the constraints between the laser range finders. In contrast to comparing a few single observations, as in [5] and [17], point registration methods can be used to align the tracks. This yields into better precision for the constraints, since not only two single matches of person detections are used for triangulation, but the whole track. For matching tracks, the following methods are applicable: Longest Common Subsequence (LCS) [20], Quaternion-based Rotationally Invariant LCS (QRLCS) [8], Levenshtein Distance on trajectories [7], or track matching based on ICP [1]. The latter is used in our approach. Also a representation of tracks as feature vectors and comparing the features [11] is possible.

The calibration algorithm presented here was developed in parallel and independently to the methods of Glas et al. [5] and Sasaki et al. [17]. The algorithm of [17] can not be compared to our approach due to insufficient evaluation in its experimental section. Also several details are are not clear and, therefore, a reimplementation was not possible. The general workflow of our method is similar to [5], but the implementation differs. As their calibration needs to run iteratively in parallel to the tracking, our algorithm can calibrate the network in only one step, after acquiring a sufficient amount of tracks. The differences between both approaches are addressed subsequently in the respective subsections.

3. Calibration

In order to calibrate the sensor network, six tasks are performed (see Fig. 1). At first, the tracks of people need to be recorded for each laser range finder (Sect. 3.1). By comparing these tracks, mutual observations between the LRF units are detected (Sect. 3.2). Based on the mutual observations, constraints between LRF units are identified (Sect. 3.3). The main calibration step is performed by resolving these constraints (Sect. 3.4). An additional relaxation algorithm is included to resolve multiple constraints (Sect. 3.5). In order to improve the calibration, a final ICP-

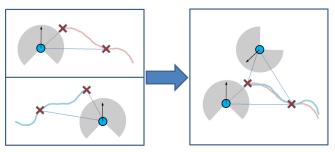


Figure 2. Aligning a pair of LRF units based on two individual observations (marked as crosses) as described in Glas et al. [5]. On the left side, both LRF units have observed a person twice. The two relating tracks are associated and the LRF units are aligned accordingly on the right side. The alignment minimizes the distance between both observations.

alignment is performed (Sect. 3.6).

3.1. Tracking

In order to obtain tracks for each person, tracking needs to be performed for each LRF in its local cartesian coordinate system. Almost any tracking method, which extracts the individual tracks of persons from laser range data in real-time [10, 18, 19], is suitable for our calibration method. The tracking algorithm we have chosen applies a histogram based background subtraction on the range data in order to get detections of people [18]. Multiple particle filters are applied to track persons independently, as described in [18].

After tracking people for an initial period, their tracks can be used to identify mutual observations between laser range finders.

3.2. Track Association

For each pair (m,n) of LRF, their tracks are compared in order to find pairs, belonging to the same person. In Glas et al. [5], the tracks are compared by their velocity profile. Since matching tracks by velocity holds more occasions for false associations as matching them by mean Euclidean error after alignment, we followed the latter approach. Not only the geometrical shapes are considered this way, but also the velocities are incorporated indirectly by the distance between two adjacent sampling points.

A track $T_a = (\mathbf{p}_{1,a}, \mathbf{p}_{2,a}, \dots, \mathbf{p}_{N,a})$ consists of N sampling points $\mathbf{p}_{i,a} = (x_{i,a}, y_{i,a}, t_i)^T$, $i = 1, \dots, N$, where $(x_{i,a}, y_{i,a})^T$ is the position of the person a at the time t_i . Before associating the tracks of two LRF, all tracks from LRF m are paired with all tracks from LRF n. Afterwards, the two tracks T_a^m and T_b^n of each pair are trimmed to the period, where they have an overlap in time. Since our sensor network is synchronized in time, the two resulting tracks \widetilde{T}_a^m and \widetilde{T}_b^n are sampled at the same time steps and have the

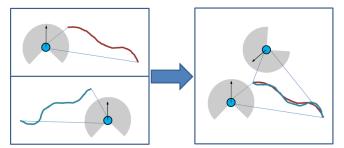


Figure 3. Aligning a pair of LRF units based on the whole observed track as implemented in our approach. On the left side, both LRF units have observed a person. The two tracks are associated, and the LRF units are aligned accordingly on the right side. The alignment minimizes the distance between all sampling points of the two tracks.

same amount of sampling points. Now, they can be easily aligned onto each other and the mean Euclidean error between their sampling points is calculated.

A track \widetilde{T}_a^m can be aligned onto another track \widetilde{T}_b^n by transforming its sampling points $\mathbf{p}_{i,a}$ to $\hat{\mathbf{p}}_{i,a}$ according to Eq. 1, with $\phi_{a,b}$ being the optimal rotation and $(x_{a,b},y_{a,b})^T$ the optimal translation.

$$\hat{\mathbf{p}}_{i,a} = \begin{pmatrix} \cos(\phi_{a,b}) & \sin(\phi_{a,b}) & 0\\ -\sin(\phi_{a,b}) & \cos(\phi_{a,b}) & 0\\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} \mathbf{p}_{i,a} - \begin{pmatrix} x_{a,b} \\ y_{a,b} \\ 0 \end{pmatrix} \end{pmatrix}$$
(1)

The optimal rotation and translation can be calculated by minimizing the mean Euclidean error $d_{a,b}$ (see Eq. 2) with an approach, introduced in [1] and [12]. It uses singular value decomposition for registering two point sets.

$$d_{a,b} = \frac{\sum_{i=1}^{N} \sqrt{(\hat{x}_{i,a} - x_{i,b})^2 + (\hat{y}_{i,a} - y_{i,b})^2}}{N}$$
(2)

After aligning two tracks \widetilde{T}_a^m and \widetilde{T}_b^n , they are considered belonging to the same person, if their error $d_{a,b}$ is below an experimentally evaluated threshold of 20 cm.

3.3. Pairing Sensors

Based on all pairs of tracks belonging to the same person, relative positions between sensor nodes can be calculated for each pair of LRF independently. Glas et al. [5], uses only the positions of people for the current iteration to constrain pairs of LRF units. With a pair of observations, the relative positions of both laser range finders can be triangulated (see Fig. 2). In contrast to this approach, we incorporated the whole tracks for alignment (see Fig. 3). At first, all matched Tracks \widetilde{T}_j^m and \widetilde{T}_j^n , $j=1,\ldots,J$ of LRF unit m and n are joined into two virtual tracks T_m and T_n

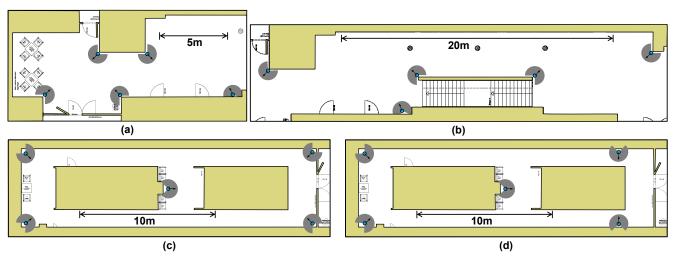


Figure 4. Overview of the four LRF setups used in our experiments. The LRF and their coverage angles are shown as gray arcs.

with Eq. 3.

$$T_m = \left(\widetilde{T}_1^m, \widetilde{T}_2^m, \dots, \widetilde{T}_J^m\right) \tag{3}$$

Since the matched Tracks are synchronized in time and are of the same length, the resulting virtual tracks are also synchronized in time and of the same length. Therefore, they can easily be aligned onto each other using the same procedure, described in 3.2. The resulting optimal rotation $\check{\phi}_{m,n}$, translation $(\check{x}_{m,n},\check{y}_{m,n})^T$ and their error $d_{m,n}$ can be used to form a constraint for the corresponding pair of laser range finders. A constraint for LRF units m and n contains the relative pose $\check{\theta}_{m,n} = \left(\check{x}_{m,n},\check{y}_{m,n},\check{\phi}_{m,n}\right)^T$ of unit m in the local space of unit n and $\check{\theta}_{n,m}$ vice versa. Additionally, a weight $w_{m,n}$ is calculated for the constraint according to Eq. 4, with N being the amount of sampling points of T_m . Long matched tracks with small errors in matching results in a higher weight than short matched tracks with big errors in matching. Therefore, the weight of a constraint depicts its confidence.

$$w_{m,n} = \frac{N}{d_{m,n}} \tag{4}$$

3.4. Pose Estimation

All LRF pairs are sorted in descending order of their weight $w_{m,n}$. One LRF unit of the pair with the highest weight is placed at the origin of the global coordinate system. The other unit is then placed corresponding to their constraint. Afterwards, every other pair containing one LRF unit, which is already placed, is aligned iteratively. If $\theta_m = (x_m, y_m, \phi_m)^T$ is the pose of a placed LRF unit, $\theta_n = (x_n, y_n, \phi_n)^T$ can be computed with Eq. 5. This is

done, until all LRF are placed.

$$\theta_n = \begin{pmatrix} \cos(-\phi_m) & \sin(-\phi_m) & 0\\ -\sin(-\phi_m) & \cos(-\phi_m) & 0\\ 0 & 0 & 1 \end{pmatrix} \cdot \check{\theta}_{n,m} + \theta_m \tag{5}$$

3.5. Relaxation

Additionally, the relaxation algorithm introduced in [3] refines all constraints iteratively, after the initial pose estimation. This procedure takes every constraint into account and, therefore, closes loops in constraints. This approach was adopted for our algorithm in order to improve the results. For each LRF m, new positions $(x_{m,n},y_{m,n})$ are estimated with Eq. 6 based on all neighboring LRF $n=1,\ldots,L$ and the corresponding constraints $\check{\theta}_{m,n}$.

$$x_{m,n} = x_n + \cos(-\phi_n) \cdot \check{x}_{m,n} + \sin(-\phi_n) \cdot \check{y}_{m,n}$$

$$y_{m,n} = y_n - \sin(-\phi_n) \cdot \check{x}_{m,n} + \cos(-\phi_n) \cdot \check{y}_{m,n}$$
(6)

Afterwards, a weight $v_{m,n}$ is calculated for each position estimate, based on the weight of each neighbor w_n and the weight $w_{m,n}$ of the corresponding constraint according to Eq. 7.

$$v_{m,n} = \frac{w_n \cdot w_{m,n}}{w_n + w_{m,n}} \tag{7}$$

After calculating all position estimates and their weights for all LRF, a new weight w_m and position (x_m, y_m) for a LRF m can be calculated with Eq. 8 and Eq. 9.

$$w_m = \sum_{n=1}^L v_{m,n} \tag{8}$$

$$x_m = \sum_{n=1}^{L} \frac{x_{m,n} \cdot v_{m,n}}{w_m} \qquad y_m = \sum_{n=1}^{L} \frac{y_{m,n} \cdot v_{m,n}}{w_m}$$
(9)

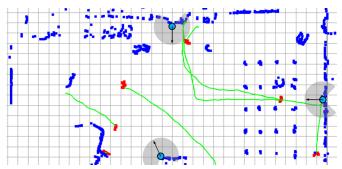


Figure 5. Calibrated scene utilizing three laser range finders at the Erfurt-Weimar airport, Germany. The background scans are colored blue and the foreground scans are colored red. The LRF and their coverage angles are shown as gray arcs. The tracks of all persons are shown green.

Finally, the rotations ϕ_m are adjusted by minimizing Eq. 10.

$$\phi_m = \underset{\phi}{\operatorname{argmin}} \left(\sum_{n=1}^{L} \left| \left(\phi + \check{\phi}_{n,m} \right) - \operatorname{atan} \left(\frac{y_n - y_m}{x_n - x_m} \right) \right| \right)$$
(10)

3.6. Final ICP Alignment

For a laser range finder, a person is only observable from one side. Therefore, the tracking mechanism may have an offset, depending of the angle from which the person is observed. This also results in an offset of the calibration. To counteract the offset and further improve the calibration accuracy, an ICP algorithm is applied on the scan points of each laser range finder. Only points classified as background by the background subtraction, mentioned in 3.1, are used for alignment. The generic ICP assigns a point from the target set to every point from the source set and performs a transformation in order to minimize the distances between them iteratively [1]. Since the overlap between laser range finders is usually small, such a procedure would seriously thwart the calibration. In contrast to the basic ICP, as presented in [1], we only take points into account, which are close to each other. This way, only scan points which may be caused by the same observed object are tightened.

4. Experiments

We already employed the calibration in several situations utilizing multiple LRF, as described in [4] and depicted in Fig. 5. Since no precise ground truth was obtainable in these situations, we conducted several experiments at our lab to evaluate the calibration performance. We recorded 13 sequences at two locations with four setups. The first location represents an open space, at which calibration yields no dif-

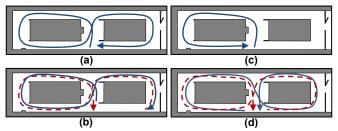


Figure 6. Walking paths in setup C and D (see Fig. 4). In (a), a single person (shown blue) walked an eight-shaped path through the corridors. In (b), two persons (shown red and blue) walked an eight-shaped path in opposite directions. In (c), a single person (shown blue) walked around the left block. In (d), two persons (shown red and blue) walked an eight-shaped path in mirrored directions.

ficulties. The second location is used to test the calibration under more challenging situations in corridors with junctions. In the first location we used two setups. Setup A (see Fig. 4(a)) covers an area of approximately $15\mathrm{m} \times 6\mathrm{m}$ where a person can be observed by every LRF at almost any time. Setup B (see Fig. 4(b)) was designed to force errors in alignment to sum up. It covers an area of approximately $30\mathrm{m} \times 6\mathrm{m}$ with the LRF placed in a chain. In the second location we also used two setups. In setup C (see Fig. 4(c)) we placed the LRF with an overlap as large as possible while covering the whole area. It is assumed, that closing loops in constraints with relaxation helps improving the calibration results. Setup D (see Fig. 4(d)) was chosen to give a more challenging situation since the overlap between the most right LRF is diminished.

4.1. Conducted Experiments

An overview of the conducted experiments is shown in Table 1. Additionally, the walking paths in setup C and D

Pattern	Setup (Fig. 4)			
	A	В	C	D
walking straight from left to				
right and back with constant speed	A1	B1		
tottering around to cover a				
large area	A2	B2		
walking with varying speed				
from left to right and back	A3			
randomly strolling around for a				
minute	A4			
one person walking an eight				
(see Fig. 6(a))			C1	D1
two persons walking an eight in				
opposite directions (see Fig. 6(b))			C2	D2
one person walking around the				
left block (see Fig. 6(c))			C3	
two persons walking an eight in				
mirrored directions (see Fig. 6(d))			C4	D3

Table 1. Overview over different setups used in our experiments. The used location and LRF placement (A to D) can be seen in Fig.4

are depicted in Fig. 6.

For the addressed setups, we used five laser range finders LMS151 from SICK. They scan 270° with a 0.5° resolution at 50 Hz with a maximum range of 50 m. The ground truth was obtained by manually measuring their positions. The LMS151 has an internal clock and tags every scan data with a timestamp, enabling us to compensate for delays, caused by the network, with time synchronization. In order to synchronize the clocks of the LRF and the receiving computer, the offset between the two clocks needs to be known. Local Area Networks usually have round-trip-times lower than the time between two laser scans, which is 20 ms. Therefore, it is sufficient to maintain the minimum offset observed between the timestamp of a laser scan and the time of reception at the computer. The residual error may be addressed with more sophisticated methods but this simple solution proved to be sufficient in our scenario.

4.2. Results and Discussion

For evaluation, each scenario was calibrated 1000 times, and the final result of every calibration belonging to one scenario was examined. The translational and rotational errors were calculated. The mean and standard deviation of all 1000 translational and rotational errors for each scene are shown in Table 2. Exemplary, the calibration error over time of a reimplementation of [5] and our approach is shown for scene B2 in Fig. 7.

In order to provide a fair comparison, we used the same synchronized data for evaluating our approach and the algorithm presented in [5].

First of all, it can be seen that our approach performs excellent in easy settings (Scene A and B in Table 2). Even in scene B, where the LRF are placed in a chain and errors may sum up, the alignment is as good as in the easier scene A. Since the calibration errors are within the measurement errors of the used type of laser range finders (systematic error of ± 3 cm and a statistical error of ± 1.2 cm), the calibration of our approach can be considered perfect in scenes A

	our approach				Glas et al. [5]			
Setup	posit	ional	rotational		positional		rotational	
	error in cm		error in °		error in cm		error in °	
	mean	std	mean	std	mean	std	mean	std
A1	2.1	0.3	0.3	< 0.1	33.5	3.9	1.0	0.5
A2	2.0	0.3	0.2	0.1	8.8	2.2	0.5	0.2
A3	1.9	0.3	0.3	< 0.1	8.1	2.0	0.5	0.3
A4	1.6	0.3	0.3	0.1	6.5	2.1	0.5	0.3
B1	1.9	0.5	0.2	< 0.1	7.5	2.6	0.5	0.2
B2	1.5	0.5	0.2	< 0.1	10.3	3.3	0.6	0.3
C1	9.2	4.7	0.7	0.6	_	_	_	_
C2	86.5	154	5.8	10.6	583	257	58.2	19.7
C3	34.8	8.2	4.4	1.5	_	_	_	_
C4	66.6	42.9	6.8	7.3	_	_	_	_
D1	47.9	26.8	3.4	2.2	_	_	_	_
D2	90.4	58.1	4.0	4.5	488	36.1	54.6	8.0
D3	29.3	20.3	3.7	7.5	561	177	38.6	15.6

Table 2. Calibration errors

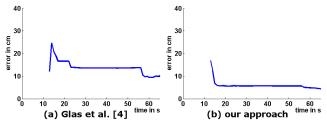


Figure 7. Calibration error of scene B2 over time. In (a), the error of the method by Glas et al. [5] is shown. In (b), the error of our approach is presented. After t=13s, all LRF have observed mutual tracks and the first alignment was done.

and B. Additionally, the rotational error is below the angular resolution of the used LRF. The method of Glas et al. [5] performs only slightly worse compared to our approach.

The algorithm presented in [5] performed poorly in scene C and D. In some cases the algorithm was not able to align all five LRF (marked with a "—"). The missing LRF was always the one standing in the middle corridor (Fig. 4(c,d)). Its overlapping areas to the other four LRF are very small, and mutual observations only appear for a short time. Since the algorithm in [5] takes observations every $1.3 \, \mathrm{s}$, there is only a small chance to sample more than one mutual observation with another LRF. Also matching tracks based on the velocities leads to more confusions as matching them by shape, as the results in C2, D2 and D3 show.

Our approach was able to obtain good calibration results in difficult scenes (C and D). The standard deviation of the alignment error shows that a few calibrations failed (C2). The tracks of both persons are similar in scene C2 (see Fig. 6(b): turning left followed by turning right). Thus, two distant LRF with no overlapping scan areas are sometimes matching their tracks by mistake due to their almost similar shape. These false matches are causing erroneous constraints leading to large errors in calibration. This problem may be addressed by observing the scene for a longer

	our approach with ICP				our approach without ICP			
Setup	posit	ional	rotational		positional		rotational	
	error in cm		error in °		error in cm		error in °	
	mean	std	mean	std	mean	std	mean	std
A1	2.1	0.3	0.3	< 0.1	5.4	0.7	0.2	0.2
A2	2.0	0.3	0.2	0.1	5.6	0.6	0.5	0.3
A3	1.9	0.3	0.3	< 0.1	4.5	0.9	0.2	0.2
A4	1.6	0.3	0.3	0.1	4.1	0.9	0.4	0.2
B1	1.9	0.5	0.2	< 0.1	4.8	1.2	0.4	0.2
B2	1.5	0.5	0.2	< 0.1	4.5	1.0	0.4	0.2
C1	9.2	4.7	0.7	0.6	10.2	5.0	1.2	0.9
C2	86.5	154	5.8	10.6	83.2	156	5.6	10.6
C3	34.8	8.2	4.4	1.5	22.0	5.8	4.0	1.3
C4	66.6	42.9	6.8	7.3	70.6	44.5	6.8	7.4
D1	47.9	26.8	3.4	2.2	45.5	26.9	2.9	2.2
D2	90.4	58.1	4.0	4.5	80.4	63.6	3.3	4.5
D3	29.3	20.3	3.7	7.5	29.4	20.7	3.4	7.3

Table 3. Influence of ICP

time. As long, as ambiguous tracks are outnumbered by unique tracks, our approach is able to calibrate correctly. In C4 and D3, the tracks of both persons are mirrored (see Fig. 6(d)). Therefore, their shapes are different, even if the velocity profile, which is used for matching in [5], is similar. Since our approach applies a track assignment incorporating the shapes, false assignments are prevented and the obtained constraints are acceptable.

We additionally calculated the positional errors before the ICP step was applied to evaluate its influence on the quality of calibration. The comparison of our approach with ICP to our approach without ICP is shown in Table 3. It can be seen that ICP improves the calibration, if a good initial estimation was found (Setup A and B). If the estimation is only moderate (Setup C and D), ICP is not always able to improve the results.

Finally, our calibration algorithm shows perfect results in ordinary situations with a lot of scan overlap (Setup A and B). In challenging situations (Setup C and D), the limits of our approach are perceivable but calibration still succeeded. The advantages of shape-based track matching and full track alignment, as used in our calibration method, could be successfully demonstrated.

5. Conclusion

We have proposed a new method for calibrating multiple LRF units into a global coordinate system by observing person tracks, without any knowledge of the scene. Furthermore, we evaluated the performance on 13 different scenes and compared it to the state of the art algorithm, presented in Glas et al. [5]. Our experiments show, that our method outperforms [5] in easy settings as well as in difficult scenes. The results in ordinary scenes can be considered to be perfect. We also conclude, that post processing the results with ICP improves the alignment.

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