Bounds for essential covers of the cube

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An essential cover of the vertices of the *n*-cube $\{-1,1\}^n$ by hyperplanes is a minimal covering where no hyperplane is redundant and every variable appears in the equation of at least one hyperplane. Linial and Radhakrishnan gave a construction of an essential cover with n/2 + 1 hyperplanes and showed that \sqrt{n} hyperplanes are required. Recently, Yehuda and Yehudayoff improved the lower bound by showing that any essential cover of the *n*cube contains at least $n^{0.52}$ hyperplanes. In this talk, we show that $n^{5/9}$ hyperplanes are needed. This is based on a joint work with Araujo and Balogh.